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## RESEARCH MEMORANDUM

EXPERIMENTAL LIFT OF LOW-ASPECT-RATIO TRIANGULAR WINGS  
AT LARGE ANGLES OF ATTACK AND SUPERSONIC SPEEDS

By William A. Hill, Jr.

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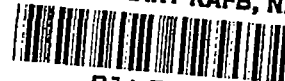
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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

RESEARCH MEMORANDUMEXPERIMENTAL LIFT OF LOW-ASPECT-RATIO TRIANGULAR WINGS  
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## SUMMARY

In order to provide information on the effects of large angles of attack on the lift and normal force on triangular wings in the Mach number range 1.96 to 3.30, three wings of aspect ratio  $3/8$ ,  $2/3$ , and 1 were tested at angles of attack up to  $47^\circ$ . The wings had modified biconvex sections in vertical streamwise planes with maximum thickness ratios of 4 percent at the 59-percent chord line and trailing edges blunted to a height one half the maximum thickness.

Near zero angle of attack the normal-force curve slopes were satisfactorily predicted by linear theory. Above angles of attack of about  $5^\circ$ , available nonlinear theories for low-aspect-ratio triangular wings were inadequate for predicting the large nonlinearities in the normal-force curves. Normal-force coefficients could be predicted, however, for angles of attack up to at least  $30^\circ$  by utilizing linear theory plus a nonlinear empirical expression for the nonlinear components of normal-force coefficients.

The data of the present investigation together with data for larger aspect ratio wings from other tests showed that the maximum lift coefficient decreased with increasing Mach number over an aspect ratio range of  $3/8$  to 4. Effects of aspect ratio became significant only below a value of about 2. The maximum lift coefficient is decreased approximately 30 percent by a decrease in aspect ratio from 2 to  $3/8$ . Maximum lift coefficient could be correlated within  $\pm 5$  percent when plotted as a function of the ratio of Mach number to aspect ratio.

## INTRODUCTION

This report is the sixth in a series on the high-incidence characteristics of wings alone and wings employed as all-movable controls in combination with a body in the Mach number range 1.45 to 3.36. Kaattari

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(refs. 1 and 2) measured the pressure distributions on a rectangular wing of aspect ratio 2 and two triangular wings of aspect ratio 2 and 4. An analysis of some of the pressure distribution data for the two triangular wings is presented by Katzen and Pitts in reference 3. In reference 4, Pitts made a detailed comparison between the experimental and theoretical loadings on three rectangular wings having aspect ratios 1, 2, and 3. All of these wings were employed as all-movable controls, as described in reference 5, by mounting them in combination with a body. The present report investigates the lift of three triangular wings of aspect ratio  $3/8$ ,  $2/3$ , and 1 at angles of attack up to  $47^\circ$ .

## SYMBOLS

|                      |  |
|----------------------|--|
| A                    | aspect ratio   |
| b                    | wing span  |
| c                    | local chord  |
| $c_r$                | root chord   |
| $C_L$                | lift coefficient, $\frac{\text{lift}}{q_\infty S}$                 |
| $C_{L_{\max}}$       | maximum lift coefficient   |
| $C_N$                | normal-force coefficient, $\frac{\text{normal force}}{q_\infty S}$ |
| $C_{N_{\text{lin}}}$ | normal-force coefficient from linear theory                        |
| M                    | Mach number  |
| $q_\infty$           | free-stream dynamic pressure                                       |
| r                    | maximum thickness of filleted root section                         |
| S                    | wing plan-form area  |
| t                    | local thickness of wing section                                    |
| $\alpha$             | angle of attack  |
| $\beta$              | $\sqrt{M^2 - 1}$   |
| $\epsilon$           | wing semiapex angle, deg   |

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## APPARATUS

The investigation was conducted in the Ames 1- by 3-foot supersonic wind tunnel No. 2. This tunnel is a nonreturn, intermittent-operation, variable-pressure wind tunnel with a Mach number range of 1.4 to 3.8. The Mach number is changed by varying the contour of flexible steel plates which form the upper and lower walls of the nozzle.

The models consisted of three triangular wings of aspect ratios  $3/8$ ,  $2/3$ , and 1. A sketch of the models with their dimensions summarized is presented in figure 1. The wings had modified biconvex sections in vertical streamwise planes with maximum thickness ratios of 4 percent at the 59-percent chord line and trailing edges blunted to a height one half of the maximum thickness. All of the wings had filleted root sections to be consistent with tests of similar wings in references 1 through 5. The maximum width of the fillet was 0.1 of the wing span. The maximum height is shown as the dimension  $r$  in figure 1. Each wing was supported from the rear by a strut which was attached to a strain-gage balance mounted in the wind tunnel. The front part of each strut was integral with its respective wing. The rear part, which was detachable from the front, was either straight for the angle-of-attack range  $0^\circ$  to  $\pm 15^\circ$ , or had a  $30^\circ$ -angle bend to increase the available range from  $+15^\circ$  to  $+45^\circ$ , or  $-15^\circ$  to  $-45^\circ$  (the latter was accomplished by rotating the model  $180^\circ$ ). The struts were attached to the wings in either a symmetrical or asymmetrical position, as shown in figure 1. The rear portion of each of the struts, downstream of the wing trailing edge, was shielded from air loads by a shroud.

## TEST PROCEDURE

Tests were conducted at Mach numbers of 1.96, 2.43, and 3.30, and at a Reynolds number per inch of 0.85 million. The maximum angle of attack varied between  $41^\circ$  and  $47^\circ$  including deflection of the supports under load. Lift, normal force, drag, and pitching-moment coefficients of each model were measured; however, effects of the model support struts on the drag and pitching-moment coefficients were found to be sufficiently large to warrant exclusion of these data from the present report. It is believed that the struts had only a small effect on lift and normal-force coefficients. An indication of this effect of the struts was obtained from comparisons of lift coefficients of the wing of aspect ratio  $3/8$  having both symmetrical and asymmetrical struts. These comparisons (fig. 2) show that at low angles of attack the lift measured with the symmetrical strut was identical with the average of the lifts obtained with the asymmetrical strut above and below the wing. At high angles of attack the lift measured with the symmetrical strut was only slightly higher than that obtained with the asymmetrical strut located on the expansion surface. The asymmetrical

strut in this location can contribute at most only a small negative lift, since it is immersed in a flow field of low pressure relative to the undisturbed stream.

#### PRECISION OF DATA

Uncertainty in the measured values of lift and normal-force coefficients was determined on the basis of repeatability, estimated effects of tunnel-stream asymmetry determined from comparisons of data measured at positive and negative angles of attack, and the uncertainty involved in evaluating the effects of the support strut. The maximum uncertainty in  $C_L$  and  $C_N$  is estimated to be less than  $\pm 0.02$ . The accuracy in measuring angle of attack is within  $\pm 0.1^\circ$ . The variation in the free-stream Mach number in the region occupied by the models was less than  $\pm 0.02$  at  $M = 1.96$ ,  $\pm 0.03$  at  $M = 2.43$ , and  $\pm 0.05$  at  $M = 3.30$ .

#### RESULTS AND DISCUSSION

Figures 2 to 4 present lift coefficient as a function of angle of attack for each of the wings. In no case was the maximum lift coefficient attained at the maximum angle of attack tested ( $\alpha = 47^\circ$ ). However, an estimate of  $C_{L_{max}}$  was obtained by a small extrapolation of each of the lift curves. The extrapolated values of  $C_L$  were obtained from a linear extrapolation of corresponding curves of  $C_L/\cos \alpha$  vs.  $\alpha$  since in the region near maximum lift coefficient  $C_L/\cos \alpha$ , which is essentially  $C_N$ , was approximately linear with  $\alpha$ . The extrapolated portions of the lift curves are shown dashed.

#### Comparisons With Data From Semispan Tests

Prior to the present investigation of full-span triangular wings of low aspect ratio, a similar investigation was conducted which employed semispan triangular wings of small span mounted on a boundary-layer bypass plate. The aspect ratios and sections of the three semispan wings were identical to those of the three wings of the present investigation. Maximum lift coefficients obtained from these semispan tests have been published in reference 6. A subsequent investigation of semispan wings in combination with a half-body (ref. 5), however, has indicated that the lift measured on semispan models of small span is subject to significant effects of interaction of the bypass-plate boundary layer with the model shock wave. Therefore, the present lift data and those obtained from tests of the three semispan models are compared in figure 5 to show the

effects of a boundary-layer bypass plate. It is evident that the lift curves of the semispan wings are noticeably lower than those of the corresponding full-span models throughout the angle-of-attack range, and particularly near  $C_{L_{max}}$ . The semispan wing of aspect ratio  $3/8$ , which experienced the largest effect of the plate, had the smallest semispan of the three models,  $3/4$  inch compared to  $1-1/2$  inches for the aspect ratio  $2/3$  and  $1$  wings. For a wing with a sufficiently large span, the plate effect on the total lift should be small. For example, references 1 and 2 present the span loadings on two wings of aspect ratio  $2$  and  $4$  mounted on the same bypass plate mentioned above. These wings had semispans of  $4$  inches. Only near  $C_{L_{max}}$  do the corresponding span load distributions of these wings show a slight decrease at the most inboard station.

#### Prediction of Lift and Normal Force and Comparison With Experiment

Several nonlinear theories (refs. 7 through 9) are available for calculating the lift of low-aspect-ratio triangular wings. These theories, however, are restricted to wings at subsonic speeds or wings with leading edges lying well within the Mach cone. The expression for lift is considered to consist of a linear term for fully attached flow plus a nonlinear viscous term. The viscous term represents the effects of flow separation from sharp leading edges and the formation of two spiral vortex sheets above the wing surface. Each vortex sheet is approximated by a concentrated vortex lying inboard of the leading edge. Several different theoretical forms of the nonlinear term have arisen. By making somewhat different assumptions as to the details of the flow model and the boundary conditions involved, Küchemann (ref. 7), Edwards (ref. 8), and Brown and Michael (ref. 9) develop the following expressions for lift:

$$C_L = C_{L_{lin}} + \frac{\pi^{3/2}}{4} A \alpha^{3/2} \quad (\text{ref. 7}) \quad (1)$$

$$C_L = C_{L_{lin}} + \pi A^{1/3} \alpha^{5/3} \quad (\text{ref. 8}) \quad (2)$$

$$C_L = C_{L_{lin}} + \pi A^{1/3} \alpha^{5/3} \left[ 1 + \frac{2}{3} \left( \frac{\alpha}{A} \right)^{2/3} \right] \quad (\text{ref. 9}) \quad (3)$$

Equations (2) and (3) were obtained by essentially the same method; however, equation (3) retains a higher order term. Comparisons of these equations with the experimental normal-force coefficients are presented in figure 6. Normal force rather than lift is compared since, for large

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angles of attack, equations (1) to (3) actually represent  $C_N$  rather than  $C_L$ . It should be noted that for the linear term references 7 to 9 use the result from slender-body theory of  $\pi\alpha/2$  (ref. 10) whereas in figure 6 the more exact linear-theory value (ref. 11) of  $(\pi\alpha/2)[1/E(k)]$  is used. The function  $E(k)$  is the normalized complete elliptic integral of the second kind of modulus  $k = \sqrt{1-\beta^2 \tan^2 \epsilon}$ . Near  $\alpha = 0$  the normal-force curve slopes are approximately those given by linear theory. At larger angles of attack the divergence of normal-force coefficients calculated by the various nonlinear methods is apparent. These comparisons also reflect the opposing trends of the theories and experiment. The nonlinear theories predict an increase in the nonlinear normal-force increment with increasing aspect ratio, while experiment shows that at a constant Mach number the normal-force increment (obtained as the difference between experimental normal-force coefficient and the corresponding linear-theory value) decreases markedly with increasing aspect ratio. Reference 12 shows this same trend of experiment at low subsonic speeds. Effects of Mach number are not considered by the various theories; however, the experimental data show a significant decrease in the normal-force increment with increasing Mach number.

These effects of Mach number and aspect ratio on the experimental normal-force increment are shown in figure 7 to correlate with the parameter  $\beta \tan \epsilon$ . For angles of attack up to at least  $30^\circ$ ,  $C_N - C_{Nlin}$  is, in general, dependent only on  $\beta \tan \epsilon$  and  $\alpha$ . As shown in figure 7 this relationship can be approximated by the empirical expression,

$$C_N - C_{Nlin} = \frac{\alpha^{3/2}}{4(\beta \tan \epsilon)^{3/4}} \quad (4)$$

for the range  $0.15 < \beta \tan \epsilon < 0.8$ . The exponent of  $\alpha$  in equation (4) is seen to be identical to that given by Kuchemann's theory (eq. (1)). Comparisons of the experimental  $C_N$  with those calculated from equation (4) are presented in figure 8. In all cases, generally good agreement is obtained between experimental and empirical values of normal-force coefficient up to angles of attack of about  $35^\circ$ .

#### Maximum Lift Coefficient

The maximum lift coefficient of each of the wings is presented in figure 9 as a function of Mach number. Maximum lift coefficient was obtained as discussed previously by a linear extrapolation of curves of  $C_L/\cos \alpha$  vs.  $\alpha$ . The plot includes additional  $C_{Lmax}$  data from references 1, 2, 13, and 14 for higher aspect ratio triangular wings. A relatively large decrease in  $C_{Lmax}$  is indicated when the aspect ratio is decreased below a value of 2; above 2, only a slight effect of aspect

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ratio on  $C_{L_{max}}$  is shown. All of the wings show approximately the same decrease in  $C_{L_{max}}$  with increasing Mach number. A simple correlation of these effects of aspect ratio and Mach number is presented in figure 10 where  $C_{L_{max}}$  is plotted as a function of the ratio of Mach number to aspect ratio. The data of the present tests and of references 1, 2, 13, and 14 are shown to lie within  $\pm 5$  percent of an average curve. The curve drawn gives the approximate result,

$$C_{L_{max}} \approx \frac{1}{(M/A)^{1/6}}$$

### CONCLUSIONS

Measurements were made in the Mach number range 1.96 to 3.30 of the lift and normal force on three triangular wings of aspect ratio 3/8, 2/3, and 1 at angles of attack up to  $47^\circ$ . An analysis of the results of this investigation has led to the following conclusions:

1. Near zero angle of attack the normal-force curve slopes are satisfactorily predicted by linear theory. Above angles of attack of about  $5^\circ$ , however, available nonlinear theories for low-aspect-ratio triangular wings are inadequate for predicting the large nonlinearities in the normal-force curves.

2. Normal-force coefficients can be predicted for angles of attack up to at least  $30^\circ$  by utilizing linear theory plus a nonlinear empirical expression for the nonlinear components of normal-force coefficients.

3. Comparisons of the maximum lift coefficients of the present report with data for larger aspect ratio wings from other investigations show that effects of aspect ratio become significant only below a value of about 2. The maximum lift coefficient decreases approximately 30 percent when the aspect ratio is decreased from 2 to 3/8.

4. For wings ranging in aspect ratio from 3/8 to 4, the maximum lift coefficient decreases with increasing Mach number.

5. Maximum lift coefficient can be correlated to within  $\pm 5$  percent when plotted as a function of the ratio of Mach number to aspect ratio.

Ames Aeronautical Laboratory  
National Advisory Committee for Aeronautics  
Moffett Field, Calif., Sept. 17, 1957



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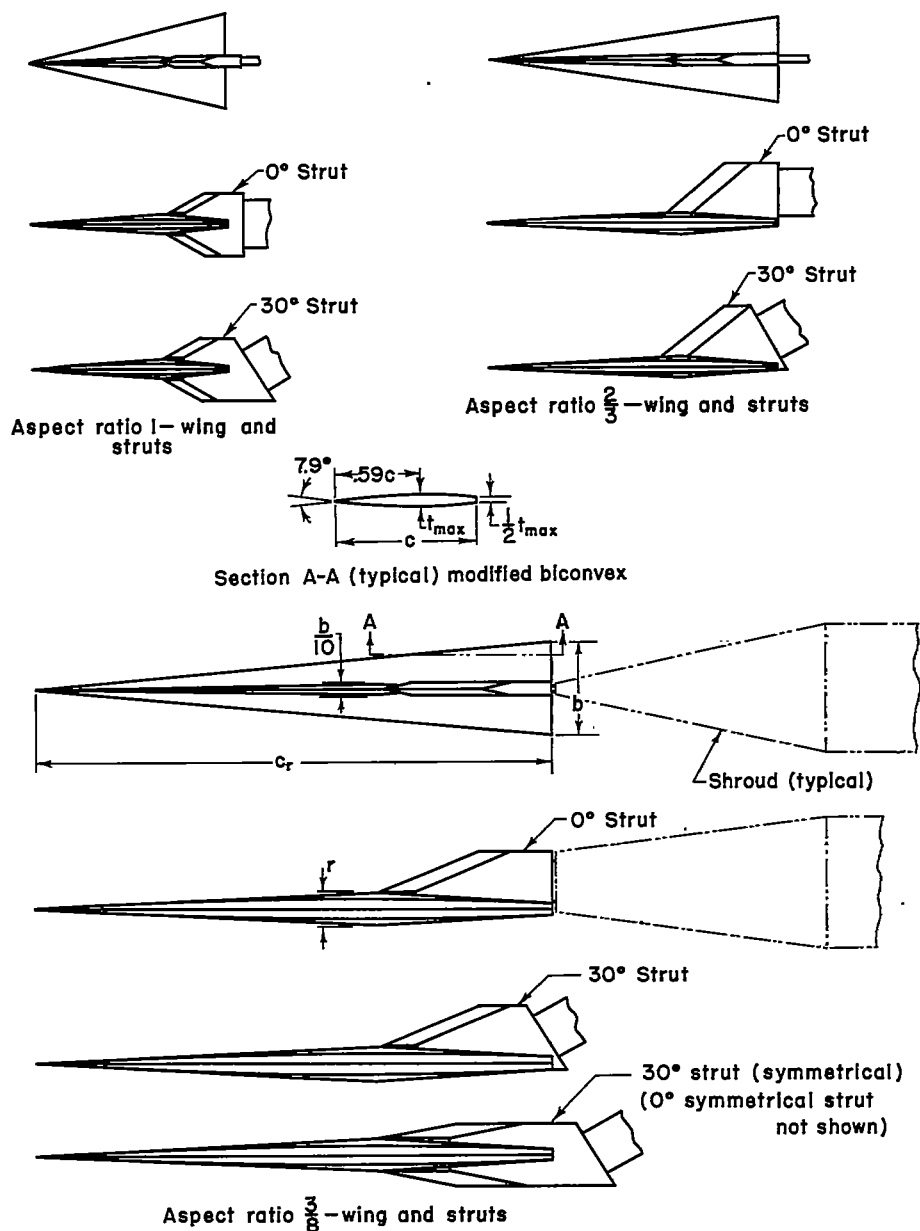


Figure 1.- Summary of model geometry and dimensions.

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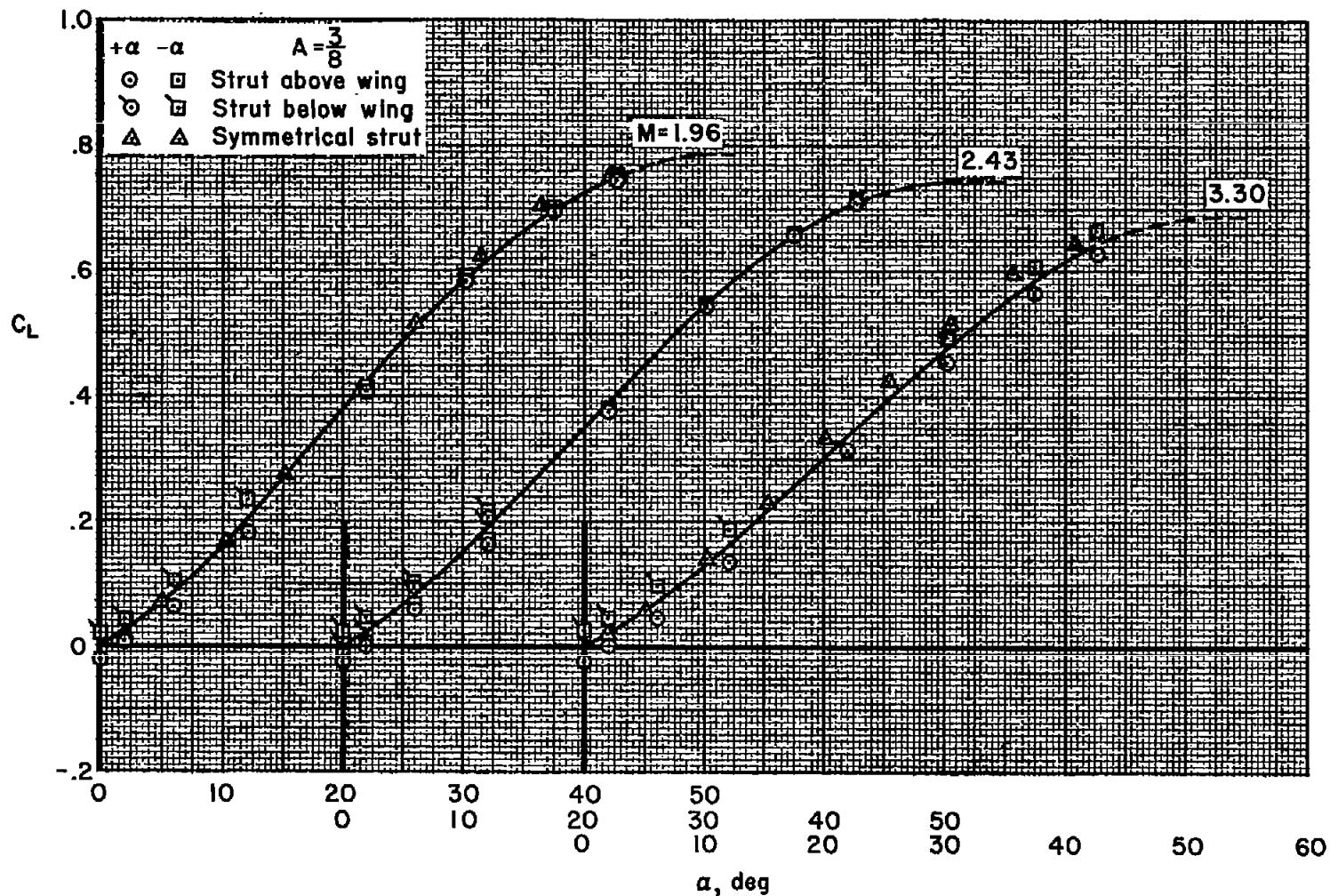


Figure 2.- Variation of lift coefficient with angle of attack for triangular wing of aspect ratio  $\frac{3}{8}$ .

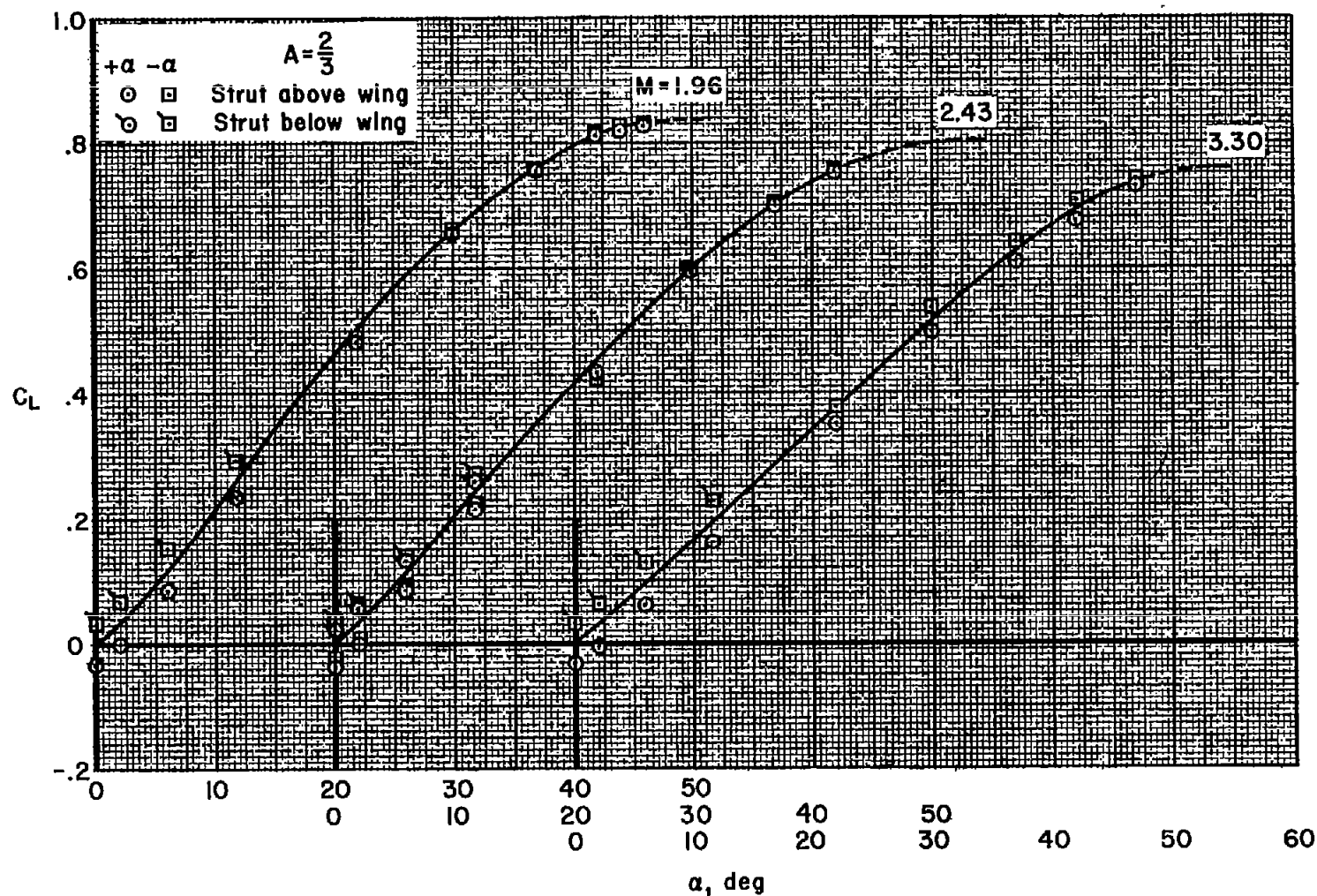


Figure 3.- Variation of lift coefficient with angle of attack for triangular wing of aspect ratio  $\frac{2}{3}$ .

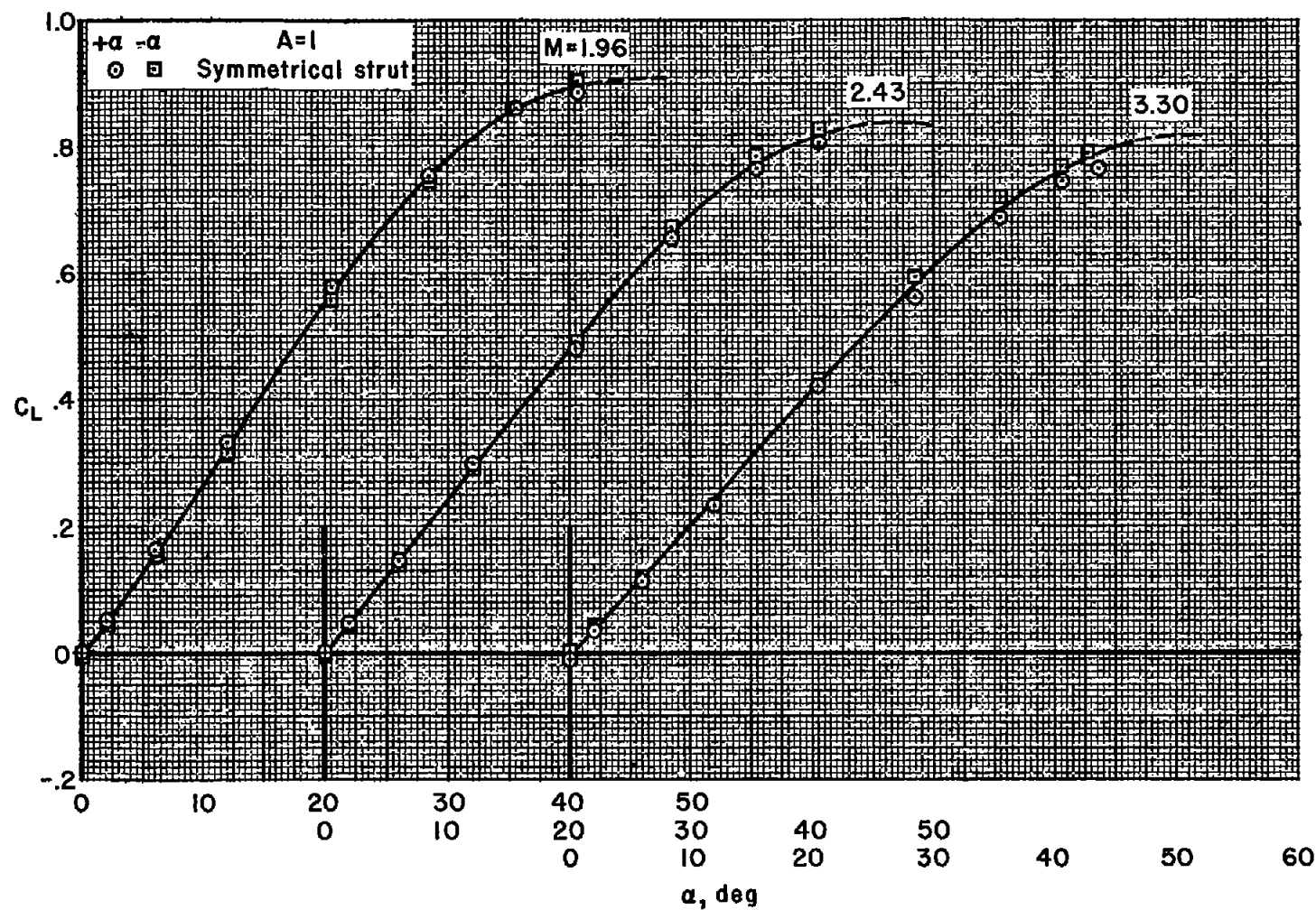
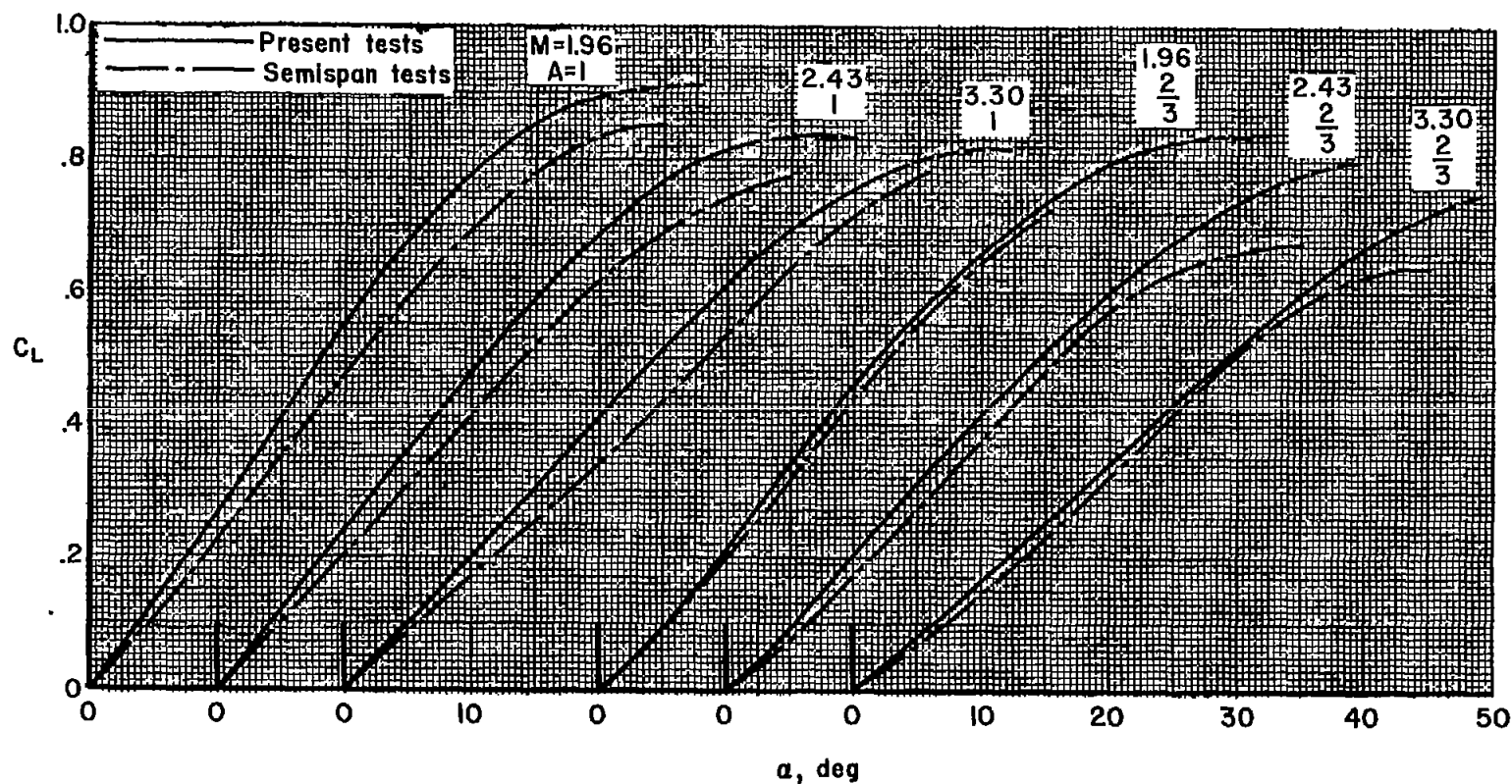


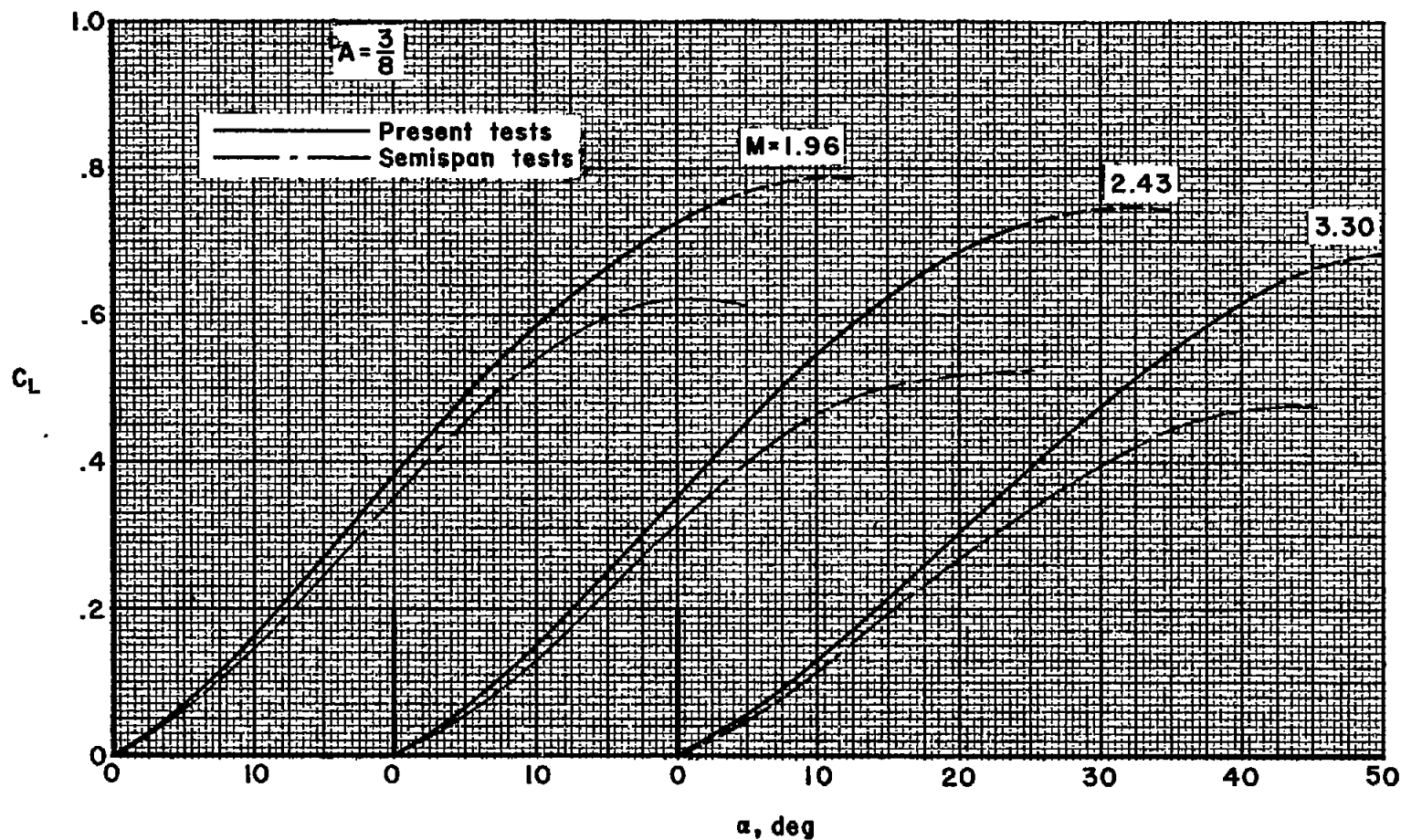
Figure 4.- Variation of lift coefficient with angle of attack for triangular wing of aspect ratio 1.



(a)  $A = 1$  and  $2/3$

Figure 5.- Comparison of the lift curves of similar full-span and semispan triangular wings.





(b)  $A = 3/8$

Figure 5.- Concluded.

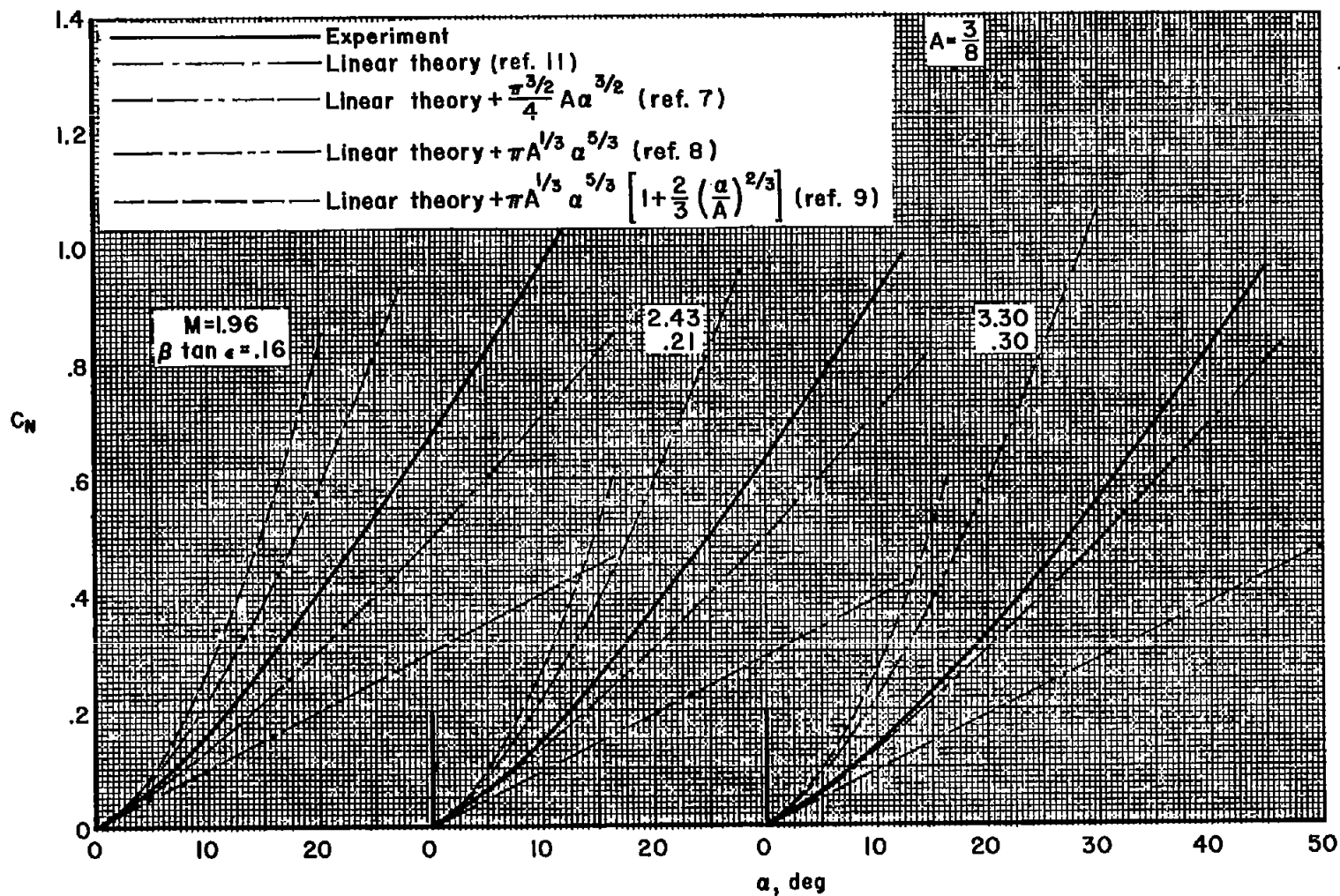
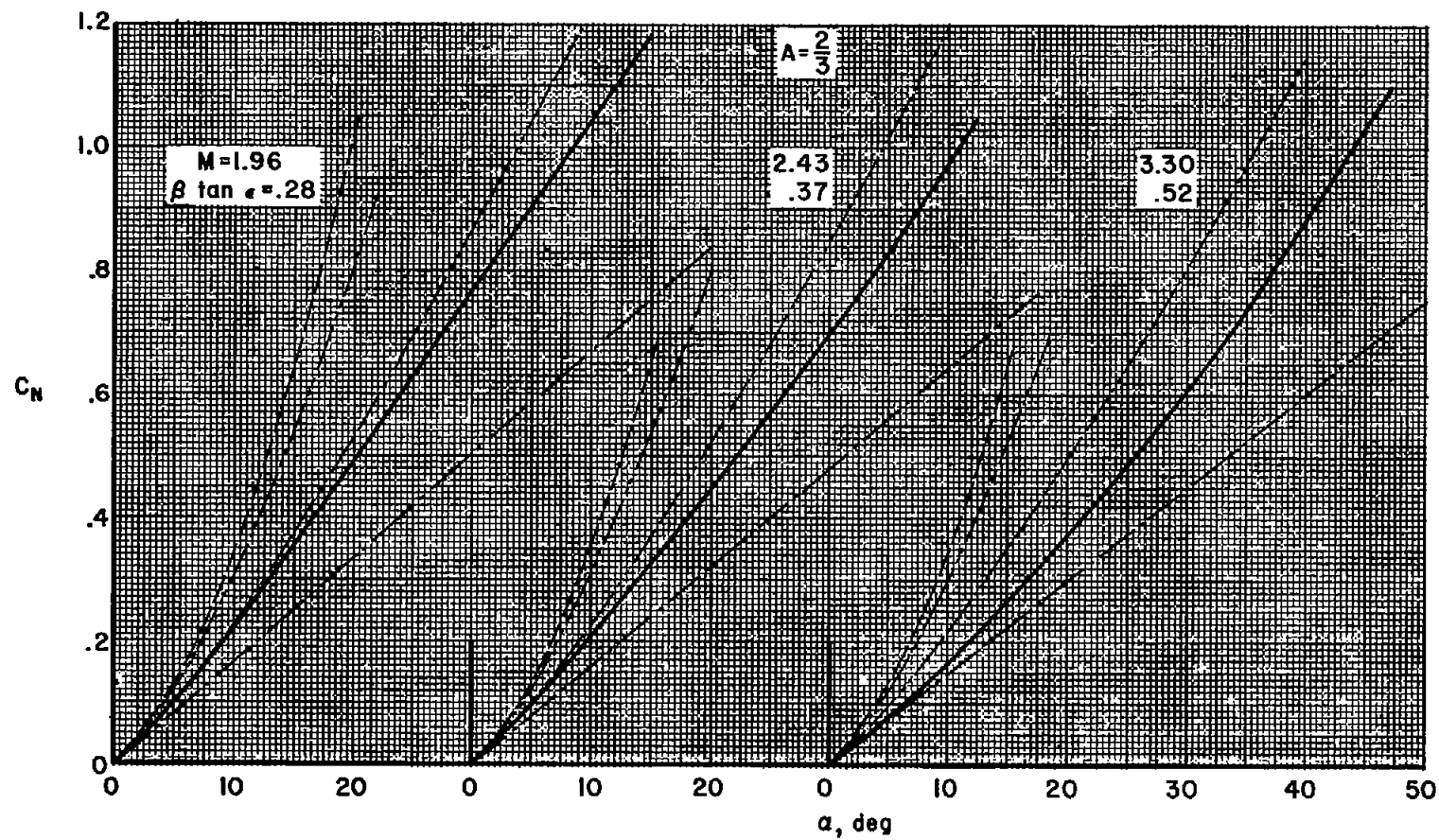
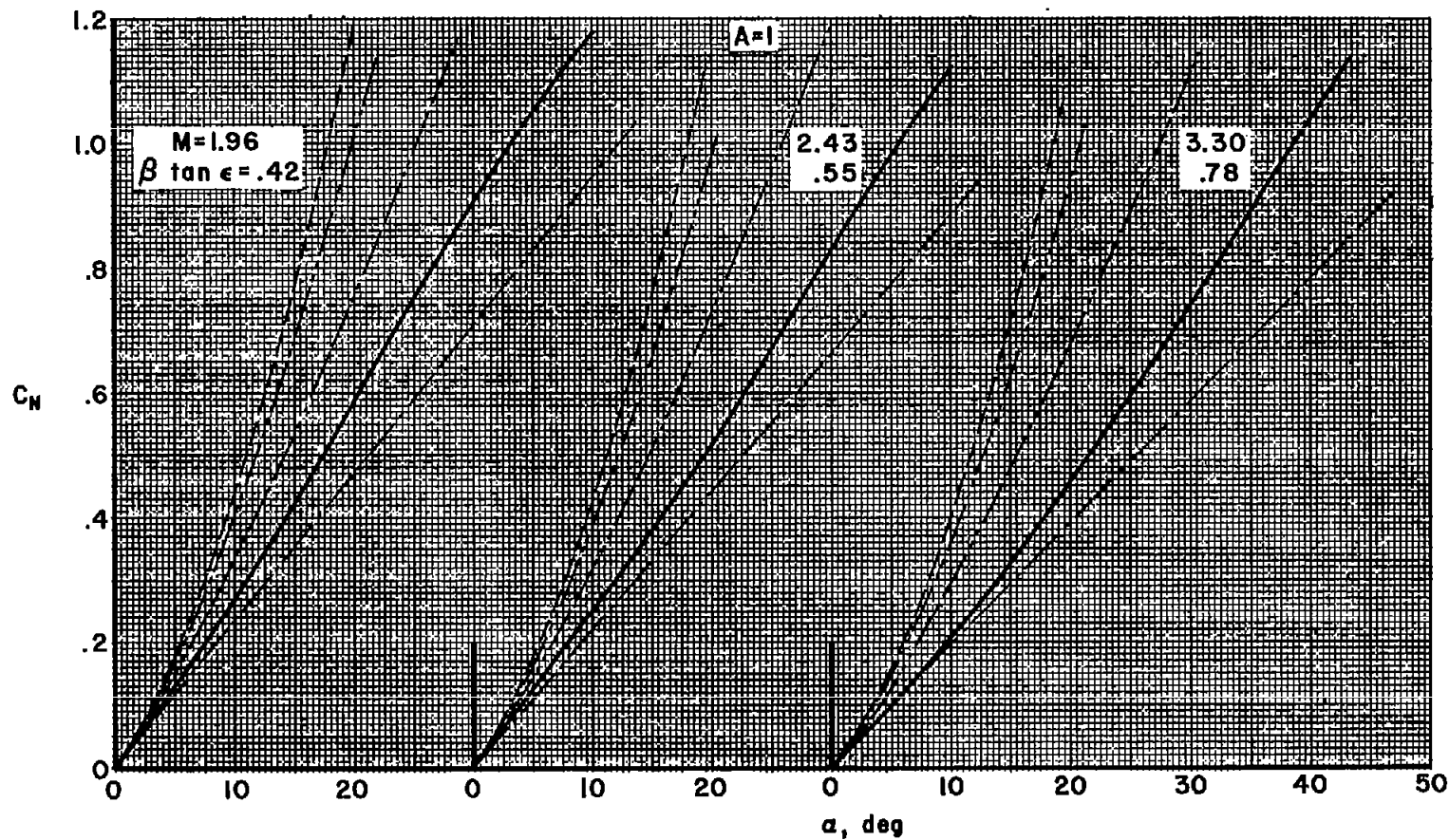
(a)  $A = 3/8$ 

Figure 6.- Comparison of experimental and theoretical values of normal-force coefficient.



(b)  $A = \frac{2}{3}$

Figure 6.- Continued.



(c)  $A = 1$

Figure 6.- Concluded.

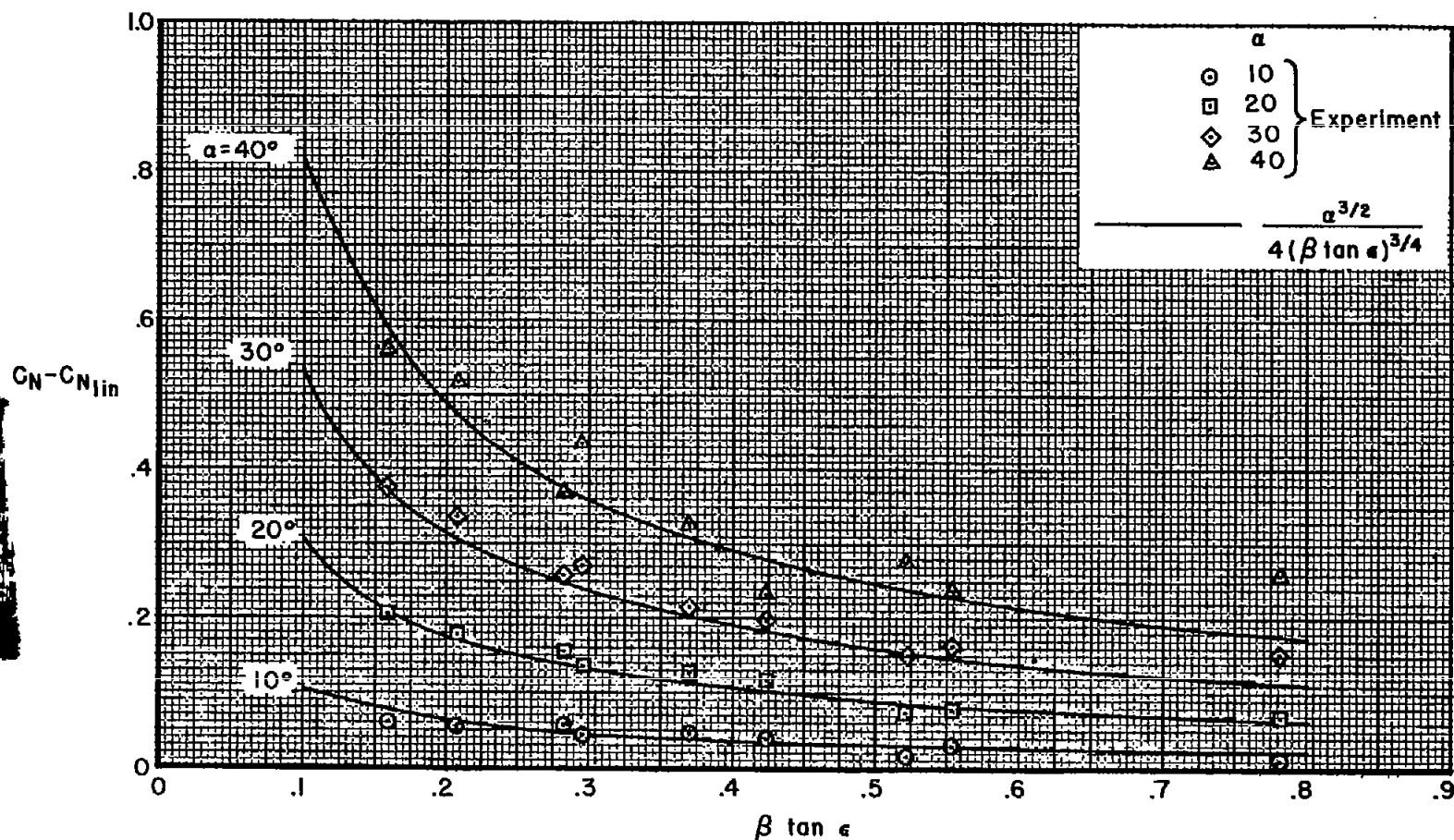


Figure 7.- Correlation of nonlinear component of normal-force coefficient with  $\beta \tan \epsilon$ .

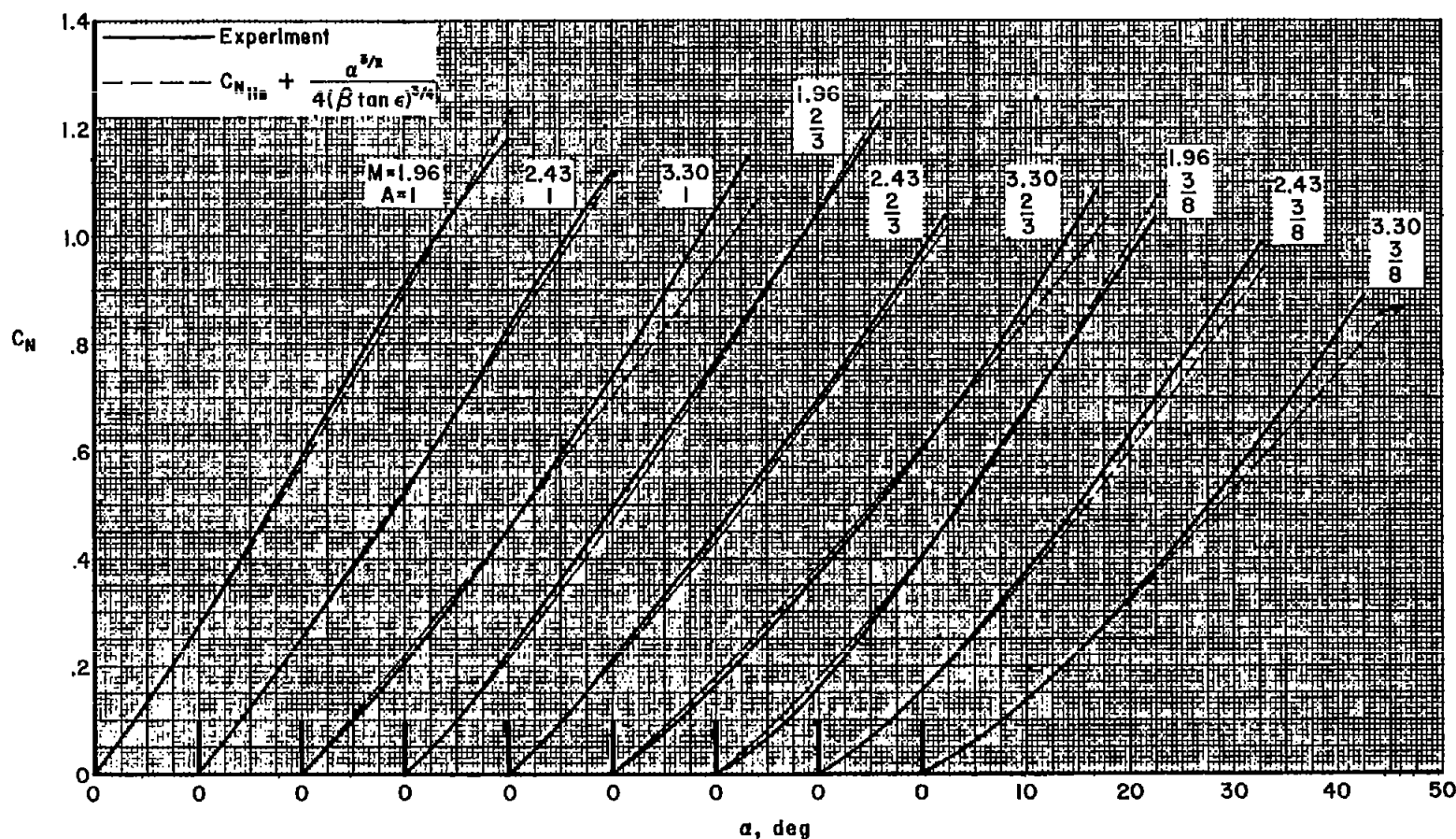


Figure 8.- Comparison of experimental and empirically predicted values of normal-force coefficient.

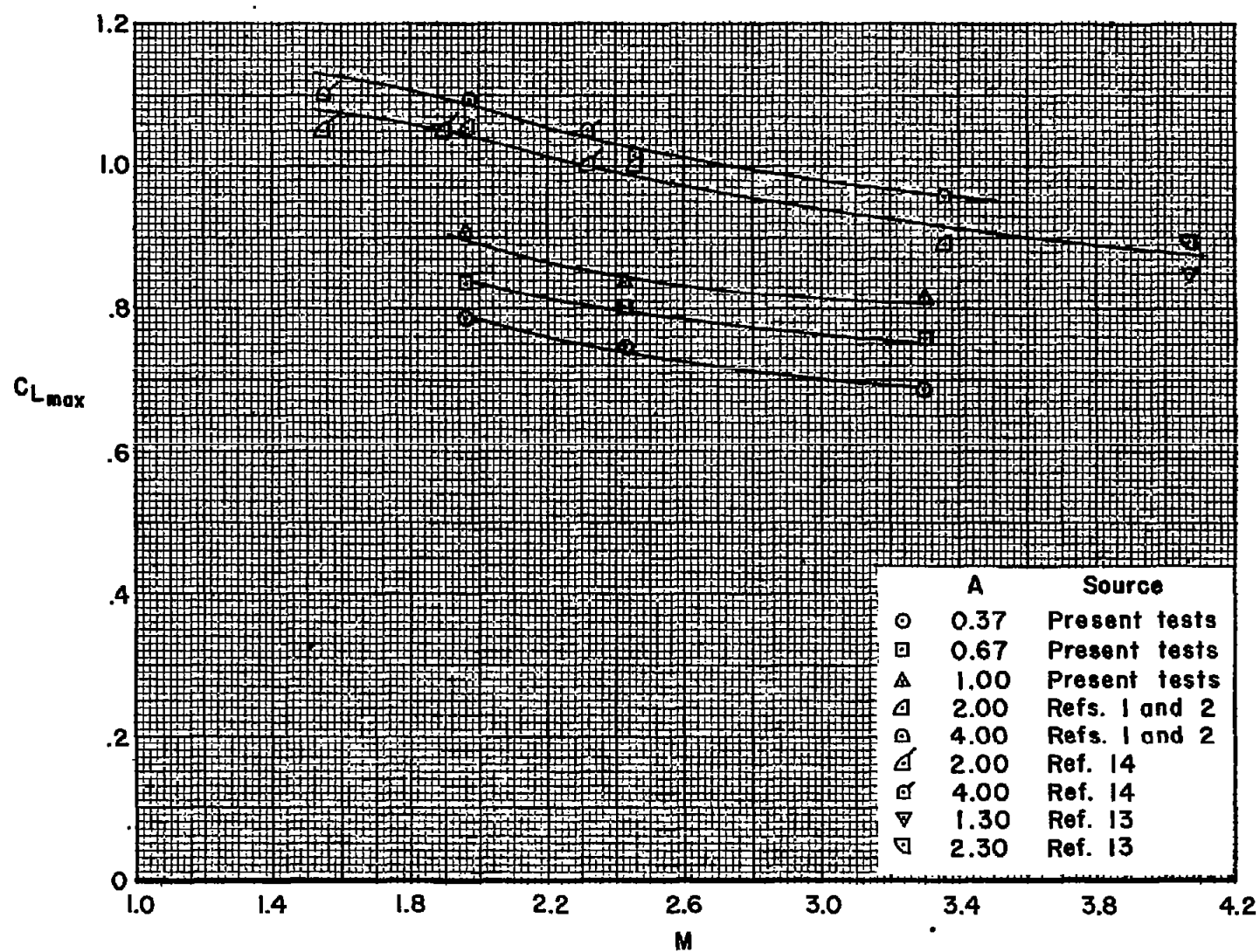


Figure 9.- Variation of maximum lift coefficient with Mach number.

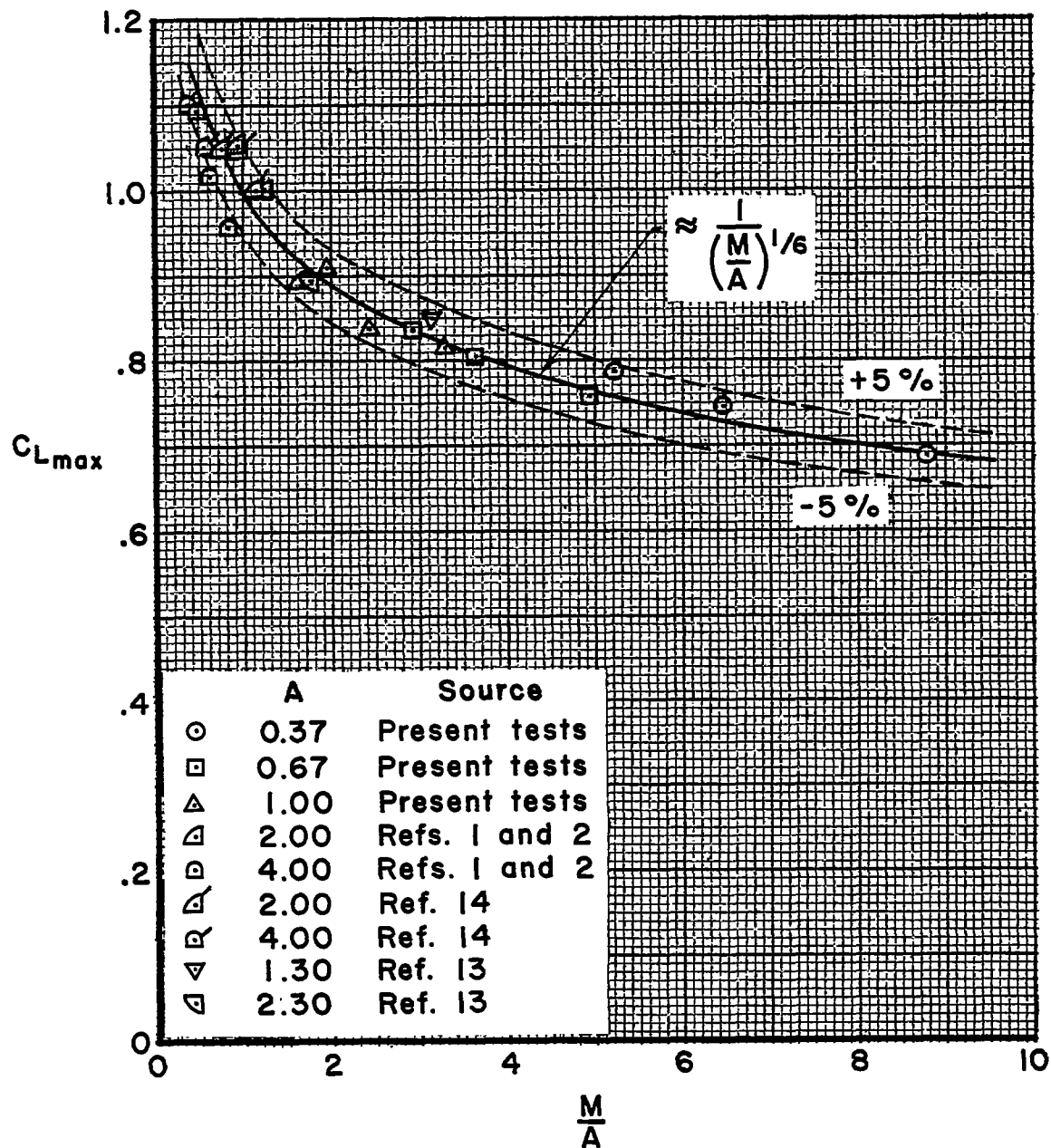


Figure 10.- Correlation of maximum lift coefficient with the ratio of Mach number to aspect ratio.